

CHAPTER - 7

SETS, **FUNCTIONS** AND ELATIONS



LEARNING OBJECTIVES

After studying this chapter, you will be able to:

- understand the concept of set theory;
- appreciate the basics of functions and relations;
- understand the types of functions and relations; and
- solve problems relating to sets, functions and relations.

In our mathematical language, everything in this universe , whether living or non-living, is called an object.

If we consider a collection of objects given in such a way that it is possible to tell beyond doubt whether a given object is in the collection under consideration or not, then such a collection of objects is called a *well-defined collection of objects*.

7.1 SETS

A set is defined to be a collection of well-defined distinct objects. This collection may be listed or described. Each object is called an element of the set. We usually denote sets by capital letters and their elements by small letters.

Example: A =
$$\{a, e, i, o, u\}$$

$$B = \{2, 4, 6, 8, 10\}$$

$$D = \{1, 3, 5, 7, 9\}$$

$$E = \{1,2\}$$

etc.

This form is called Roster or Braces form . In this form we make a list of the elements of the set and put it within braces $\{\ \}$.

Instead of listing we could describe them as follows:

$$C$$
 = The set of all possible arrangements of the letters p, q and r

E = The set of roots of the equation
$$x^2-3x + 2 = 0$$

B =
$$\{x : x = 2m \text{ and } m \text{ being an integer lying in the interval } 0 < m < 6\}$$

D =
$$\{2x - 1 : 0 < x < 6 \text{ and } x \text{ is an integer}\}$$

$$E = \{x : x^2 - 3x + 2 = 0\}$$



This form is called set-Builder or Algebraic form or Rule Method. This method of writing the set is called Property method. The symbol : or/reads 'such that'. In this method , we list the property or properties satisfied by the elements of the set.

We write, $\{x:x \text{ satisfies properties } P \}$. This means, "the set of all those x such that x satisfies the properties P"

A set may contain either a finite or an infinite number of members or elements. When the number of members is very large or infinite it is obviously impractical or impossible to list them all. In such case.

we may write as:

N = The set of natural numbers = $\{1, 2, 3, \ldots\}$

 $W = The set of whole numbers = \{0, 1, 2, 3, ...\}$

etc.

- I. The members of a set are usually called elements, In $A = \{a,e,i,o,u\}$, a is an element and we write aî A i.e. a belongs to A. But 3 is not an element of $B = \{2, 4, 6, 8, 10\}$ and we write $3 \notin B$. i.e. 3 does not belong to B.
- II. If every element of a set P is also an element of set Q we say that P is a subset of Q. We write P i Q . Q is said to be a superset of P. For example {a, b} i {a, b, c}, {2, 4, 6, 8, 10} i N. If there exists even a single element in A, which is not in B then A is not a subset of B
- III. If P is a subset of Q but P is not equal to Q then P is called a proper subset of Q.
- IV. F has no proper subset.

Illustration: $\{3\}$ is a proper subset of $\{2, 3, 5\}$. But $\{1, 2\}$ is not a subset of $\{2, 3, 5\}$.

Thus if $P = \{1, 2\}$ and $Q = \{1, 2, 3\}$ then P is a subset of Q but P is not equal to Q . So , P is a proper subset of Q.

To give completeness to the idea of a subset, we include the set itself and the empty set. The empty set is one which contains no element. The empty set is also known as **null or void** set usually denoted by $\{\}$ or Greek letter F, to be read as phi. For example the set of prime numbers between 32 and 36 is a null set. The subsets of $\{1, 2, 3\}$ include $\{1, 2, 3\}$, $\{1, 2\}$, $\{1, 3\}$, $\{2, 3\}$, $\{1\}$, $\{2\}$, $\{3\}$ and $\{\}$

A set containing n elements has 2ⁿ subsets. Thus a set containing 3 elements has

 2^3 (=8) subsets. A set containing n elements has 2^n –1 proper subsets. Thus a set containing 3 elements has 2^3 –1 (=7) subsets. The proper subsets of { 1,2,3} include

$$\{1, 2\}$$
, $\{1, 3\}$, $\{2, 3\}$, $\{1\}$, $\{2\}$, $\{3\}$, $\{\}$.

Suppose we have two sets A and B. The intersection of these sets, written as AI B contains those elements which are in A and are also in B.

For example $A = \{2, 3, 6, 10, 15\}$, $B = \{3, 6, 15, 18, 21, 24\}$ and $C = \{2, 5, 7\}$,

we have $A \cap B = \{3, 6, 15\}$, $A \cap C = \{2\}$, $B \cap C = \Phi$, where the intersection of B and C is empty

set. So, we say B and C are disjoint sets since they have no common element. Otherwise sets are called overlapping or intersecting sets. The union of two sets, A and B, written as AUB contain all these elements which are in either A or B or both.

$$AUC = \{2, 3, 5, 6, 7, 10, 15\}$$

A set which has at least one element is called non-empty set . Thus the set $\{\,0\,\}$ is non-empty set. It has one element say 0.

Singleton Set: A set containing one element is called Singleton Set. For example

{ 1 } is a singleton set, whose only member is 1.

Equal Set : Two sets A & B are said to be equal, written as A = B if every element of A is in B and every element of B is in A.

Illustration: If $A = \{ 2, 4, 6 \}$ and $B = \{ 2, 4, 6 \}$ then A = B.

Remarks: (I) The elements of a set may be listed in any order.

Thus,
$$\{1, 2, 3\} = \{2, 1, 3\} = \{3, 2, 1\}$$
 etc.

(II) The repetition of elements in a set is meaningless.

Example : $\{x : x \text{ is a letter in the word "follow"}\} = \{f,o,l,w\}$

Example : Show that Φ , $\{0\}$ and \emptyset are all different.

Solution: Since Φ is a set containing no element at all; $\{0\}$ is a set containing one element, namely 0. And 0 is a number , not a set.

Hence F, $\{0\}$ and 0 are all different.

The set which contains all the elements under consideration in a particular problem is called *the universal set* denoted by S. Suppose that P is a subset of S. Then the complement of P, written as P^c (or P') contains all the elements in S but not in P. This can also be written as S - P or S - P. $S - P = \{x : x \hat{1} \ s, x \hat{1} \ p\}$.

For example let $S = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

$$P = \{0, 2, 4, 6, 8\}$$

$$Q = \{1, 2, 3, 4, 5\}$$

Then
$$P' = \{1, 3, 5, 7, 9\}$$
 and $Q' = \{0, 6, 7, 8, 9\}$

Also
$$P \cup Q = \{0, 1, 2, 3, 4, 5, 6, 8\}, (P \cup Q)^1 = \{7, 9\}$$

$$P \cap Q = \{2, 4\}$$

$$P \cup Q' = \{0, 2, 4, 6, 7, 8, 9\}, (P \cap Q)' = \{0, 1, 3, 5, 6, 7, 8, 9\}$$



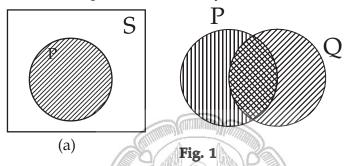
$$P' \cup Q' = \{ 0,1, 3, 5, 6, 7, 8, 9 \}$$

$$P' \cap Q' = \{7, 9\}$$

So it can be noted that $(P \cup Q)' = P' \cap Q'$ and $(P \cap Q)' = P' \cup Q'$. These are known as De Morgan's laws.

7.2 VENN DIAGRAMS

We may represent the above operations on sets by means of Euler -Venn diagrams.

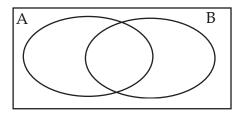


Thus Fig. 1(a) shows a universal set S represented by a rectangular region and one of its subsets P represented by a circular shaded region.

The un-shaded region inside the rectangle represents P'.

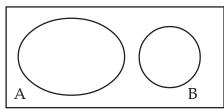
Figure 1(b) shows two sets P and Q represented by two intersecting circular regions. The total shaded area represents PUQ, the cross - hatched "intersection" represents $P \cap Q$.

The number of distinct elements contained in a finite set A is called its **cardinal number**. It is denoted by n(A). For Example , the number of elements in the set $R = \{2, 3, 5, 7\}$ is denoted by n(R). This number is called the cardinal number of the set R.

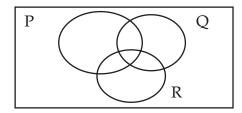


Thus $n(AUB) = n(A) + n(B) - n(A \cap B)$

If A and B are disjoint sets, then n(AUB) = n(A) + n(B) as $n(A \cap B) = 0$







For three sets P, Q and R

$$n(PUQUR) = n(P) + n(Q) + n(R) - n(P \cap Q) - n(Q \cap R) - n(P \cap R) + n(P \cap Q \cap R)$$

When P,Q and R are disjoint sets

$$n(P \cup Q \cup R) = n(P) + n(Q) + n(R)$$

Illustration: If
$$A = \{ 2, 3, 5, 7 \}$$
, then $n(A) = 4$

Equivalent Set : Two finite sets A & B are said to be equivalent if
$$n(A) = n(B)$$
.

Clearly, equal sets are equivalent but equivalent sets need not be equal.

Illustration: The sets $A = \{1, 3, 5\}$ and $B = \{2, 4, 6\}$ are equivalent but not equal.

Here n(A) = 3 = n(B) so they are equivalent sets. But the elements of A are not in B. Hence they are not equal though they are equivalent.

Power Set: The collection of all possible subsets of a given set A is called the power set of A, to be denoted by P(A).

Illustration: (I) If $A = \{1, 2, 3\}$ then

$$P(A) = \{ \{1, 2, 3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1\}, \{2\}, \{3\}, \{6\} \} \}$$

(II) If
$$A = \{ 1, \{2\} \}$$
, we may write $A = \{ 1, B \}$ when $B = \{2\}$ then

$$P(A) = \{_{\Phi} \ , \ \{1\} \ , \{B\} \} \ , \ \{\ 1,B\} \} = \{_{\Phi} \ , \ \{\ 1\} \ , \{\ 2\} \ \} \ , \ \{\ 1,\{2\} \} \}$$

Exercise 7 (A)

Choose the most appropriate option or options (a), (b) (c) and (d)

- 1. The number of subsets of the set $\{2, 3, 5\}$ is
 - (a) 3,
- (b) 8,

(c) 6,

- (d) none of these,
- 2. The number of subsets of a set containing n elements is
 - (a) 2^n
- (b) 2^{-n}

(c) n

(d) none of these

- 3. The null set is represented by
 - $(a)\{\Phi \}$
- (b) { 0 }
- (c) Φ

- (d) none of these
- 4. $A = \{2, 3, 5, 7\}$, $B \{4, 6, 8, 10\}$ then $A \cap B$ can be written as
 - (a) { }
- (b) $\{\Phi\}$

- (c) (AUB)'
- (d) None of these
- 5 The set $\{x \mid 0 < x < 5\}$ represents the set when x may take integral values only



	(a) {0, 1, 2, 3, 4, 5	(b) {1, 2, 3, 4 }	c) {1, 2, 3, 4, 5 }	(d) none of these
6.	The set {0, 2, 4, 6}	, 8, 10} can be written as	S	
	(a) $\{2x \mid 0 < x < 5\}$	(b) $\{x : 0 < x < 5\}$	(c) $\{2x : 0 \le x \le 5\}$	(d) none of these
	If P = {1, 2, 3, 5, 7	7}, Q = {1, 3, 6, 10, 15}, U	Iniversal Set $S = \{1, 2, 3\}$, 4, 5, 6, 7, 8, 9, 10, 11, 12,
	13, 14, 15}			
7.	The cardinal num	nber of PI Q is		
	(a) 3,	(b) 2	(c) 0	(d) none of these
8.	The cardinal num	nber of PUQ is		
	(a) 10,	(b) 9,	(c) 8,	(d) none of these
9.	$n(P^1)$ is			
	(a) 10,	(b) 5,	(c) 6,	(d) none of these
10.	$n(Q^1)$ is			
	(a) 4,	(b) 10,	(c) 4,	(d) none of these
11.	The set of cubes of	of the natural number is		
	(a) a finite set,	(b) an infinite set,	(c) a null set	(d) none of these
12.	The set $\{2^x \mid x \text{ is an}\}$	ny positive rational num	nber J is	
	(a) an infinite set,	, (b) a null set,	(c) a finite set,	(d) none of these
13.	$\{1-(-1)^x\}$ for all in	ntegral x is the set	reta article	
	(a) {0},	(b) {2},	(c) {0,2}	(d) none of these
14.	E is a set of positi	ive even number and O	is a set of positive odd	numbers, then $E \cup O$ is a
	(a) set of whole n	umbers, (b) N,	(c) a set of rational nu	mber, (d) none of these
15.	If R is the set of p	oositive rational number	and E is the set of real	numbers then
	(a) R <u>C</u> E,	(b) R C E	(c) E C R	(d) none of these
16.	If N is the set of r	natural numbers and I is	s the set of positive inte	gers, then
	(a) $N = I$,	(b) N Ì I,	(c) N <u>C</u> I,	(d) none of these
17.0	If I is the set of is	osceles triangles and E i	s the set of equilateral t	riangles, then
	(a) IÌ E,	(b) EÌ I,	(c) E=I	(d) none of these
18.	If R is the set of is	sosceles right angled tria	angles and I is set of iso	sceles triangles, then
	(a) $R = I$	(b) R 1L	(c) R'Ì I	(d) none of these

(c) is an empty set

(d) none of these

(b) an infinite set

19. $\{n(n+1)/2 : n \text{ is a positive integer} \}$ is

20. If $A = \{1, 2, 3, 5, 7\}$, and $B = \{x^2 : x \in A\}$

(a) a finite set



- (a) n(b) = n(A),
- (b) n(B) > n(A)
- (c) n(A) = n(B)
- (D) n(A) < n(B)

- 21. $A \cup A$ is equal to
 - a) A,
- (b) E,

(c) **o**

(d) none of these

- 22. $A \cap A$ is equal to
 - (a) ¢
- (b) A,

(c) E,

(d) none of these

- 23. $(A \cup B)'$ is equal to
 - (a) $(A \cap B)'$
- (b) A∪B'
- (c) $A' \cap B'$,
- (d) none of these

- 24. $(A \cap B)'$ is equal to
 - (a) (A'∪B)'
- (b) A'∪ B'
- (c) $A' \cap B'$,
- (d) none of these

- 25. $A \cup E$ is equal to (E is a superset of A)
 - (a) A,
- (b) E,

(c) ϕ ,

-(c) **o**

(c) 2E,

(d) none of these

- 26. $A \cap E$ is equal to
 - (a) A
- (b) E,

(d) none of these

- 27. EUE is equal to
 - (a) E,
- (b) ¢,
- 28. $A \cap E'$ is equal to
 - (a) E
- $(b) \phi$,

(d) none of these

(d) none of these

- 29. $A \cap F$ is equal to
 - (a) A
- (b) E

(c)

(d) none of these

- 30. AUA' is equal to
 - (a) E
- $(b) \phi$,

(c) A,

- (d) none of these
- 31. If $E = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, the subset of E satisfying 5 + x > 10 is
 - (a) {5, 6, 7, 8, 9} (b) {6, 7, 8, 9},
- (c) {7, 8, 9},
- (d) none of these
- 32. If $A\Delta B = (A-B) \cup (B-A)$ and $A = \{1, 2, 3, 4\}$, $B = \{3,5,7\}$ than $A\Delta B$ is
 - (a) {1, 2, 4, 5, 7} (b) {3}
- (c) {1, 2, 3, 4, 5, 7}
- (d) none of these

[Hint: If A and B are any two sets, then

 $A - B = \{ x : x \in A, x \notin B \}.$

i.e. A - B Contains all elements of A but not in B].



7.9

7.3 PRODUCT SETS

Ordered Pair : Two elements a and b, listed in a specific order, form an ordered pair, denoted by (a, b).

Cartesian Product of sets : If A and B are two non-empty sets, then the set of all ordered pairs (a, b) such that a belongs to A and b belongs to B , is called the Cartesian product of A and B, to be denoted by $A \times B$.

Thus, $A \times B = \{ (a, b) : a \in A \text{ and } b \in B \}$

If $A = \Phi$ or B = F, we define $A \times B = \Phi$

Illustration: Let $A = \{1, 2, 3\}, B = \{4, 5\}$

Then $A \times B = \{ (1, 4), (1, 5), (2, 4), (2, 5), (3, 4), (3, 5) \}$

Example: If $A \times B = \{ (3, 2), (3, 4), (5, 2), (5, 4) \}$, find A and B.

Solution: Clearly A is the set of all first co-ordinates of $A \times B$, while B is the set of all second co-ordinates of elements of $A \times B$.

Therefore $A = \{3, 5\}$ and $B = \{2, 4\}$

Example : Let $P = \{1, 3, 6\}$ and $Q\{3, 5\}$

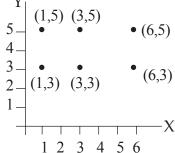
The product set $P \times Q = \{(1, 3), (1, 5), (3, 3), (3, 5), (6, 3), (6, 5)\}$.

Notice that $n(P \times Q) = n(P) \times n(Q)$ and ordered pairs (3,5) and (5,3) are not equal. and $Q \times P = \{(3, 1), (3, 3), (3, 6), (5, 1), (5, 3), (5, 6)\}$

So $P \times Q \neq Q \times P$; but $n(P \times Q) = n(Q \times P)$.

Illustration: Here n(P) = 3 and n(Q) = 2, $n(P \times Q) = 6$ Hence $n(P \times Q) = n(p) \times n(Q)$. and $n(P \times Q) = n(Q \times P) = 6$.

We can represent the product set of ordered pairs by points in the XY plane.



If X=Y= the set of all natural numbers, the product set X, Y is represented by an infinite equal lattice of points in the first quadrant of the XY plane.



7.4 RELATIONS AND FUNCTIONS

Any subset of the product set XY is said to define a **relation** from X to Y and any relation from X to Y in which no two different ordered pairs have the same first element is called a **function**.

Let A and B be two non-empty sets. Then, a rule or a correspondence f which associates to each element x of A, a unique element, denoted by f(x) of B, is called a function or **mapping** from A to B and we write $f: A \rightarrow B$

The element f(x) of B is called the image of x, while x is called the pre-image of f(x).

7.5 DOMAIN & RANGE OF A FUNCTION

Let $f: A \rightarrow B$, then A is called the domain of f, while B is called the co-domain of f.

The set $f(A) = \{ f(x) : x \in A \}$ is called the range of f.

Illustration: Let $A = \{ 1, 2, 3, 4 \}$ and $B = \{1, 4, 9, 16, 25 \}$

We consider the rule $f(x) = x^2$. Then f(1) = 1; f(2) = 4; f(3) = 9 & f(4) = 16.

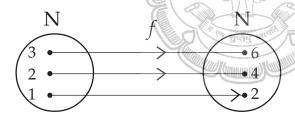
Then clearly each element in A has a unique image in B.

So, $f : A \rightarrow B : f(x) = x^2$ is a function from A to B.

Here domain (f) = $\{1, 2, 3, 4\}$

and range $(f) = \{1, 4, 9, 16\}$

Example: Let N be the set of all natural numbers. Then , the rule



 $f: N \rightarrow N: f(x) = 2x$, for all $x \in N$

is a function from N to N , since twice a natural number is unique.

Now, f(1) = 2; f(2) = 4; f(3) = 6 and so on.

Here domain (f) = $N = \{1, 2, 3, 4, \dots \}$; range (f) = $\{2, 4, 6, \dots \}$

This may be represented by the mapping diagram or arrow graph .

7.6 VARIOUS TYPES OF FUNCTION

One - one Function : Let $f: A \rightarrow B$. If different elements in A have different images in B, then f is said to be a one-one or an injective function or mapping.

Illustration: (i) Let $A = \{ 1, 2, 3 \}$ and $B = \{ 2, 4, 6 \}$

Let us consider $f : A \rightarrow B : f(x) = 2x$.

Then f(1) = 2; f(2) = 4; f(3) = 6.



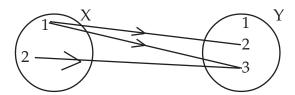
Clearly, f is a function from A to B such that different elements in A have different images in B. Hence f is one -one.

Remark: Let $f: A \rightarrow B$ and let $x_1, x_2 \in A$.

Then $x_1 = x_2$ implies $f(x_1) = f(x_2)$ is always true.

But $f(x_1) = f(x_2)$ implies $x_1 = x_2$ is true only when f is one-one.

(ii) let $x=\{1, 2, 3, 4\}$ and $y=\{1, 2, 3\}$, then the subset $\{(1, 2), (1, 3), (2, 3)\}$ defines a relation on x.y.



Notice that this particular subset contains all the ordered pair in x.y for which the X element (x) is less than the Y element (y). So in this subset we have X<Y and the relation between the set, is "less than". This relation is not a function as it includes two different ordered pairs (1,2), (1,3) have same first element.

The subset $\{(1, 1), (2, 2), (3, 3)\}$ defines the function y = x as different ordered pairs of this subset have different first element.

Onto or Surjective Functions : Let $f: A \rightarrow B$. If every element in B has at least one pre-image in A , then f is said to be an onto function.

If f is onto , then corresponding to each $y \in B$, we must be able to find at least one element $x \hat{1}$ A such that y = f(x)

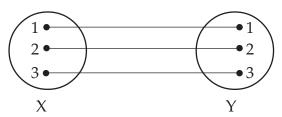
Clearly, f is onto if and only if range (f) = B

Illustration : Let N be the set of all natural numbers and E be the set of all even natural numbers. Then, the function

$$f: N \to E: f(x) = 2x$$
, for all $x \in N$

is onto, since each element of E is of the form 2x , where $x \in \ensuremath{N}$ and the same is the

f-image of $x \in N$.



Represented on a mapping diagram it is a one-one mapping of X onto Y.

Bijection Function : A one-one and onto function is said to be bijective.



A bijective function is also known as a one-to-one correspondence.

Identity Function: Let A be a non-empty set. Then, the function I defined by

 $I: A \rightarrow A: I(x) = x$ for all $x \in A$ is called an identity function on A.

It is a one-to-one onto function with domain A and range A.

Into Functions: Let $f: A \to B$. There exists even a single element in B having no pre-image in A , then f is said to be an into function.

Illustration: Let A = { 2, 3, 5, 7 } and B = { 0, 1, 3, 5, 7}. Let us consider f : A \rightarrow B;

$$f(x) = x - 2$$
. Then $f(2) = 0$; $f(3) = 1$; $f(5) = 3 & f(7) = 5$.

It is clear that f is a function from A to B.

Here there exists an element 7 in B, having no pre-mage in A.

So, f is an into function.

Constant Function: Let $f: A \to B$, defined in such a way that all the elements in A have the same image in B, then f is said to be a constant function.

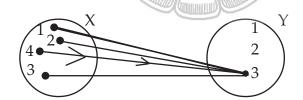
Illustration: Let $A = \{1, 2, 3\}$ and $B = \{5, 7, 9\}$. Let $f : A \rightarrow B : f(x) = 5$ for all $x \in A$.

Then, all the elements in A have the same image namely 5 in B.

So, f is a constant function.

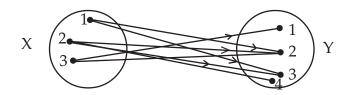
Remark: The range set of a constant function is a singleton set.

Example: Another subset of x.y is $\{(1,3), (2,3), (3,3), (4,3)\}$

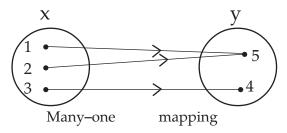


This relation is a function (a constant function). It is represented on a mapping diagram and is a many-one mapping of X into Y.

Let us take another subset $\{(4,1), (4,2), (4,3)\}$ of X.Y. This is a relation but not a function. Here different ordered pairs have same first element so it is not a function.



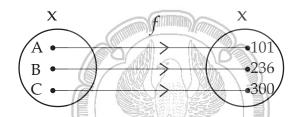




This is an example of many - one mapping.

Equal Functions: Two functions f and g are said to be equal, written as f = g if they have the same domain and they satisfy the condition f(x) = g(x), for all x.

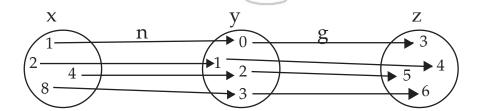
A function may simply pair people and the corresponding seat numbers in a theatre. It may simply associate weights of parcels with portal delivery charge or it may be the operation of squaring , adding to doubling, taking the log of etc.



The function f here assigning a locker number to each of the persons A, B and C. Names are associated with or mapped on to, locker numbers under the function f.

We can write

$$f: X \rightarrow Y$$
 OR, $f(x) = y$ OR, $f(B) = 236$



This diagram shows the effect of two functions n and g on the sets X, Y and Z

$$n: X \rightarrow Y \text{ and } g: Y \rightarrow Z$$

If x, y, z are corresponding elements of X, Y and Z, we write n(x) = y and g(y) = z

Thus n(1) = 0 and g(0) = 3, so that g(n(1)) = g(0) = 3 we can write it as

$$g n(1) \text{ or } g \text{ o } n (1) = 3 \text{ But } g(1) = 4 \text{ and } n(g(1)) = n(4) = 2$$

So $gn \neq ng$ (or, $g \circ n \neq n \circ g$)



The function gn or ng is called a composite function. As n(8) = 3, we say that 3 is the image of 8 under the mapping (or function) n.

Inverse Function: Let f be a one-one onto function from A to B. Let y be an arbitrary element of B. Then f being onto, there exists an element x in A such that f(x) = y.

As f is one-one this x is unique.

Thus for each $y \hat{I} B$, there exists a unique element $x \in A$ such that f(x) = y.

So, we may define a function, denoted by f⁻¹ as:

$$f^{-1}: B \rightarrow A: f^{-1}(y) = x \text{ if and only if } f(x) = y.$$

The above function f⁻¹ is called the inverse of f.

A function is invertible if and only if f is one-one onto.

Remarks : If f is one -one onto then f^{-1} is also one-one onto.

Illustration : If $f : A \rightarrow B$ then $f^{-1} : B \rightarrow A$.

Exercise 7(B)

Choose the most appropriate option/options (a), (b), (c) or (d)

- 1. If $A = \{x, y, z\}$, $B = \{p, q, r, s\}$ Which of the relation on A.B are function.
 - (a) $\{n, p\}$, (x, q), (y, r), $(z, s)\}$, (b) $\{(x, s), (y, s), (z, s)\}$
- - (c) $\{(y, p), (y, q), (y, r), (z, s), (d) \{(x, p), (y, r), (z, s)\}$
- 2. $\{(x,y) \mid x+y=5\}$ is a
- (a) not a function (b) a composite function (c) one-one mapping (d) none of these
- 3. $\{(x, y) | x = 4\}$ is a
 - (a) not a function (b) function
- (c) one-one mapping
- (d) none of these

- 4. $\{(x, y), y=x^2\}$ is
 - (a) not a function (b) a function
- (c) inverse mapping
- (d) none of these

- 5. $\{(x, y) | x < y\}$ is
 - (a) not a function (b) a function
- (c) one-one mapping
- (d) none of these

- The domain of $\{(1,7), (2,6)\}$ is
 - (a) (1, 6)
- (b) (7, 6)
- (c) (1, 2)
- (d) {6, 7}

- The range of $\{(3,0), (2,0), (1,0), (0,0)\}$ is
 - (a) {0, 0}
- (b) {0}

- $(c) \{0, 0, 0, 0\}$
- (d) none of these

- The domain and range of $\{(x,y): Y = x^2\}$ is
 - (a) (reals, natural numbers)
- (b) (reals, positive reals)

(c) (reals, reals)

(d) none of these



9.	Let the domain of	f x be the set $\{1\}$. Which	of the following function	ons are equal to 1			
	(a) $f(x) = x^2$, $g(x) = x^2$	= x	(b) $f(a) = x$, $g(x) = 1-x$				
	(c) $f(x) = x^2 + x + 2$	$g(x) = (x+1)^2$	(d) none of these				
10.	If $f(x) = 1/1-x$, $f(-1)$	-1) is					
	(a) 0	(b) ½	(c) 0	(d) none of these			
11.	If $g(x) = (x-1)/x$,	g(-1/2) is					
	(a) 1	(b) 2	(c) 3/2	(d) 3			
12.	If $f(x) = 1/1 - x$ an	d g(x) = (x-1)/x, than f	$\log(x)$ is				
	(a) x	(b) $1/x$	(c) -x	(d) none of these			
13.	If $f(x) = 1/1 - x$ and	d g(x) = (x-1)/x, then g	g of(x) is				
	(a) x-1	(b) x	(c) 1/x	(d) none of these			
14.	The function $f(x)$	$= 2^x$ is					
	(a) one-one mapp	ping	(b) one-many				
	(c) many-one		(d) none of these				
15.	The range of the f	function $f(x) = \log_{10}(1 +$	x) for the domain of rea	l values of x when $0 \notin x$			
	£9 is						
	(a) $\{0, -1\}$	(b) {0, 1, 2}	(c) {0.1}	(d) none of these			
16.	The Inverse funct	ion f^{-1} of $f(x) = 2x$ is	क्लेंबु जार				
	(a) 1/2x	(b) $\frac{x}{2}$	(c) 1/x	(d) none of these			
17.	If $f(x) = x+3$, $g(x)$	= x^2 , then fog(x) is					
	(a) $x^2 + 3$	(b) $x^2 + x + 3$	(c) $(x+3)^2$	(d) none of these			
18.	If $f(x) = x+3$, $g(x)$	$= x^2$ then $f(x)$.	g(x) is				
	(a) $(x+3)^2$	(b) x^2+3	(c) x^3+3x^2	(d) none of these			
19.	The Inverse h ⁻¹ w	then $h(x) = \log_{10} x$ is					
	(a) $\log_{10} x$	(b) 10 ^x	(c) $\log_{10}(1/x)$	(d) none of these			
20.	For the function h	$h(x) = 10^{1+x}$ the domain	of real values of x where	e $0 \le x \le 9$, the range is			

(a) $10 \le h(x) \le 10^{10}$ (d) none of these (b) $0 \le h(x) \le 10^{10}$ (c) 0 < h(x) < 10

Different types of relations

Let $S = \{a, b, c,\}$ be any set then the relation R is a subset of the product set $S \times S$

i) If R contains all ordered pairs of the form (a, a) in S×S, then R is called reflexive. In a *reflexive* relation 'a' is related to itself .

For example, 'Is equal to' is a reflexive relation for a = a is true.

ii) If $(a, b) \in R \Rightarrow (b,a) \in R$ for every $a, b \in S$ then R is called symmetric

For Example $a=b \Rightarrow b=a$. Hence the relation 'is equal to' is a symmetric relation.

iii) If $(a, b) \in R$ and $(b, c) \in R \Rightarrow (a, c) \Rightarrow R$ for every $a, b, c, \in S$ then R is called *transistive*.

For Example a =b, $b=c \Rightarrow a=c$. Hence the relation 'is equal to' is a transitive relation.

A relation which is reflexive, symmetric and transitive is called an *equivalence relation* or simply an *equivalence*. 'is equal to' is an equivalence relation.

Similarly, the relation " is parallel to " on the set S of all straight lines in a plane is an equivalence relation.

Illustration: The relation " is parallel to " on the set S is

- (1) reflexive, since a || a for a \in S
- (2) symmetric, since a \parallel b \Rightarrow b \parallel a
- (3) transitive, since a \parallel b , b \parallel c \Rightarrow a \parallel c

Hence it is an equivalence relation.

Domain & Range of a relation : If R is a relation from A to B, then the set of all first coordinates of elements of R is called the domain of R, while the set of all second co-ordinates of elements of R is called the range of R.

So, Dom (R) = {
$$a : (a, b) \in R$$
 } & Range (R) = { $b : (a, b) \in R$ }

Illustration: Let $A = \{1, 2, 3\}$ and $B = \{2, 4, 6\}$

Then
$$A \times B = \{(1,2), (1, 4), (1, 6), (2, 2), (2, 4), (2, 6), (3, 2), (3, 4), (3, 6)\}$$

By definition every subset of $A \times B$ is a relation from A to B.

Thus, if we consider the relation

$$R = \{ (1, 2), (1, 4), (3, 2), (3, 4) \}$$
 then Dom (R) = {1,3} and Range (R) = {2, 4}

From the product set X. $Y = \{(1, 3), (2, 3), (3, 3), (4, 3), (2, 2), (3, 2), (4, 2), (1, 1), (2, 1), (3, 1), (4, 1)\}$, the subset $\{(1, 1), (2, 2), (3, 3)\}$ defines the relation 'Is equal to', the subset $\{(1, 3), (2, 3), (1, 2)\}$ defines 'Is less than', the subset $\{(4, 3), (3, 2), (4, 2), (2, 1), (3, 1), (4, 1)\}$ defines 'Is greater than' and the subset $\{(4, 3), (3, 2), (4, 2), (2, 1), (3, 1), (4, 1), (1, 1), (2, 2), (3, 3)\}$ defines to greater 'In greater than or equal'.



Illustration: Let $A = \{1, 2, 3\}$ and $b = \{2, 4, 6\}$

Then $A \times B = \{(1, 2), (1, 4), (1, 6), (2, 2), (2, 4), (2, 6), (3, 2), (3, 4), (3, 6)\}$

If we consider the relation = $\{(1, 2), (1, 4), (3, 4)\}$ then Dom (R) = $\{1, 3\}$ and Range = $\{2, 4\}$ Here the relation "Is less than".

Identity Relation: The relation $I = \{(a, a) : a \in A\}$ is called the identity relation on A.

Illustration: Let $A = \{1, 2, 3\}$ then $I = \{(1, 1), (2, 2), (3, 3)\}$

Inverse Relation: If R be a relation on A, then the relation R⁻¹ on A, defined by

 $R^{-1} = \{ (b, a) : (a, b) \in R \}$ is called an inverse relation on A.

Clearly, Dom (R^{-1}) = Range (R) & Range (R^{-1}) = Dom (R).

Illustration: Let $A = \{1, 2, 3\}$ and $R = \{(1, 2), (2, 2), (3, 1), (3, 2)\}$

Then R being a subset of a \times a , it is a relation on A. Dom (R) = {1, 2, 3} and Range (R) = {2,1}

Now, $R^{-1} = \{(2, 1), (2, 2), (1, 3), (2, 3)\}$ Here, Dom $(R^{-1}) = \{2, 1\}$ = Range (R) and

Range $(R^{-1}) = \{1, 2, 3\} = Dom(R)$.

Illustration: Let $A = \{1, 2, 3\}$, then

(i) $R1 = \{(1, 1), (2, 2), (3, 3), (1, 2)\}$

Is reflexive and transitive but not symmetric, since $(1, 2) \in R$, but (2, 1) does not belong to R_1 .

(ii) $R2 = \{(1, 1), (2, 2), (1, 2), (2, 1)\}$

is symmetric and transitive but not reflexive, since (3, 3) does not belong to R_2 .

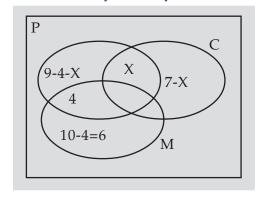
(iii) R3 = $\{(1, 1), (2, 2), (3, 3), (1, 2), (2, 1), (2, 3), (3, 2)\}$

is reflexive and symmetric but not transitive, since $(1, 2) \in \mathbb{R}3 \& (2, 3) \in \mathbb{R}3$ but

(1, 3) does not belong to R3.

Problems and solution using Venn Diagram

1. Out of a group of 20 teachers in a school, 10 teach Mathematics, 9 teach Physics and 7 teach Chemistry. 4 teach Mathematics and Physics but none teach both Mathematics and Chemistry. How many teach Chemistry and Physics? How many teach only Physics?



Let x be the no. of teachers who teach both Physics & Chemistry.

$$9-4-x+6+7-x+4+x=20$$

or
$$22-x=20$$

or x=2

Hence, 2 teachers teach both Physics and Chemistry and 9-4-2=3 teachers teach only Physics.

A survey shows that 74% of the Indians like grapes, whereas 68% like bananas.

What percentage of the Indians like both grapes and bananas?

Solution: Let P & Q denote the sets of Indians who like grapes and bananas respectively. Then n(P) = 74, n(Q) = 68 and $n(P \cup Q) = 100$.

We know that $n(P \cap Q) = n(P) + n(Q) - n(P \cup Q) = 74 + 68 - 100 = 42$.

Hence, 42% of the Indians like both grapes and bananas.

- In a class of 60 students, 40 students like Maths, 36 like Science, and 24 like both the subjects. Find the number of students who like
 - (i) Maths only.
- (ii) Science only
- (iii) either Maths or Science
- (iv) neither Maths nor Science.

Solution: Let M = students who like Maths and S = students who like Science

Then n(M) = 40, n(S) = 36 and n (M \cap S) = 24

Hence, (i) $n(M) - n(M \cap S) = 40 - 24 = 16 = number of students like Maths only.$

- (ii) $n(S) n(M \cap S) = 36 24 = 12 = number of students like Science only.$
- (iii) $n(M \cup S) = n(M) + n(S) n(M \cap S) = 40 + 36 24 = 52 = number of students who like either$ Maths or Science.
- (iv) $n(M \cup S)^c = 60 n(M \cup S) = 60 52 = 8 = number of students who like neither Maths nor$ Science.

Exercise 7C

Choose the most appropriate option/options (a), (b), (c) or (d)

- "Is smaller than" over the set of eggs in a box is

 - a) Transitive (T) (b) Symmetric (S)
- (c) Reflexive (R)
- (d) Equivalence (E)
- "Is equal to" over the set of all rational numbers is
 - (a) (T)
- (b) (S)

(c) (R)

(d) E



3.	"has the same fath	ner as" over the set	of children	
	(a) R	(b) S	(c) T	(d) none of these
4.	"is perpendicular	to " over the set of straig	ght lines in a given pla	ne is
	(a) R	(b) S	(c) T	(d) E
5.	"is the reciprocal of	of" over the set of	non-zero real numbers	s is
	(a) S	(b) R	(c) T	(d) none of these
6.	$(x,y)/x \in x, y \in y,$	y = x is		
	(a) R	(b) S	(c) T	(d) none of these
7.	$\{(x,y) / x + y = 2x$	where x and y are posi	tive integers}, is	
	(a) R	(b) S	(c) T	(d) E
8.	"Is the square of"	over n set of real numbe	ers is	
	(a) R	(b) S	(c) T	(d) none of these
9.	If A has 32 elemen	ts, B has 42 elements an	d AUB has 62 elements	s, the number of elements
	in $A \cap B$ is			
	(a) 12	(b) 74	(c) 10	(d) none of these
10	In a group of 20 ch drinking coffee bu	ıt not tea is		a. The number of children
	(a) 6	(b) 7	(c) 1	(d) none of these
11	The number of su	bsets of the sets {6, 8, 11) is	
	(a) 9	(b) 6	(c) 8	(d) none of these
12.	The sets $V = \{x / x \}$ if x is equal to	$x+2=0$, $R={x / x^2+2x=0}$	and $S = \{x : x^2 + x - 2 = 0\}$	are equal to one another
	(a) -2	(b) 2	(c) ½	(d) none of these
13.	If the universal set then	$t E = \{x \mid x \text{ is a positive i} \}$	nteger <25 }, A = $\{2, 6, 8\}$	8, 14, 22}, B = {4, 8, 10, 14}
	(a) $(A \cap B)' = A' \cup B$	B' (b) $(A \cap B)' = A' \cap B'$	(c) $(A' \cap B)' = \varphi$	(d) none of these
14.	If the set P has 3 e	elements, Q four and R	two then the set P×Q×	R contains
	(a) 9 elements	(b) 20 elements	(c) 24 elements	(d) none of these
15.	Given $A = \{2, 3\}$, I	$B = \{4, 5\}, C = \{5, 6\} \text{ then}$	$A \times (B \cap C)$ is	
		(b) {(5, 2), (5, 3)}		(d) none of these

7.19

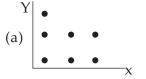


- 16. A town has a total population of 50,000. Out of it 28,000 read the newspaper X and 23000 read Y while 4000 read both the papers. The number of persons not reading X and Y both
 - (a) 2000
- (b) 3000
- (c) 2500
- (d) none of these
- 17. If $A = \{1, 2, 3, 5, 7\}$ and $B = \{1, 3, 6, 10, 15\}$. Cardinal number of $A \sim B$ is
 - (a) 3
- (b) 4

(c) 6

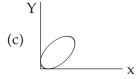
(d) none of these

18. Which of the diagram is graph of a function











- 19. At a certain conference of 100 people there are 29 Indian women and 23 Indian men. Out of these Indian people 4 are doctors and 24 are either men or doctors. There are no foreign doctors. The number of women doctors attending the conference is
 - (a) 2
- (b) 4

(c) 1

- (d) none of these
- 20. Let $A = \{a, b\}$. Set of subsets of A is called power set of A denoted by P(A). Now n(P(A)) is
 - (a) 2
- (b) 4

(c)/3

- (d) none of these
- 21. Out of 2000 employees in an office 48% preferred Coffee (c), 54% liked (T), 64% used to smoke (S). Out of the total 28% used C and T, 32% used T and S and 30% preferred C and S, only 6% did none of these. The number having all the three is
 - (a) 360
- (b) 300

- (c) 380
- (d) none of these
- 22. Referred to the data of Q. 21 the number of employees having T and S but not C is
 - (a) 200
- (b) 280

- (c) 300
- (d) none of these
- 23. Referred to the data of Q. 21. the number of employees preferring only coffee is
 - (a) 100
- (b) 260

- (c) 160
- (d) none of these

- 24. If f(x) = x+3, $g(x) = x^2$, then gof(x) is
 - (a) $(x+3)^2$
- (b) x^2+3
- (c) $x^2(x+3)$,
- (d) none of these

- 25. If f(x) = 1/1-x, then $f^{-1}(x)$ is
 - (a) 1-x
- (b) x-1/x
- (c) x/x-1
- (d) none of these



ANSWERS

Exe	Exercise 7(A)														
1.	b	2.	a	3.	С	4.	a	5.	b	6.	С	7.	b	8.	С
9.	a	10.	b	11.	b	12.	a	13.	С	14.	b	15	b	16.	a
17.	b	18.	С	19.	b	20.	a	21.	a	22.	b	23.	С	24.	b
25.	b	26.	a	27.	a	28.	b.	29.	С	30.	b	31.	b.	32.	a
Exercise 7(B)															
1.	b,d	2.	C	3.	a	4.	b	5.	a	6.	С	7.	b	8.	b
9.	a	10.	b	11.	d	12.	a	13.	b	14.	a	15.	С	16.	b
17.	a	18.	С	19.	b	20.	a.								
Exe	rcise	7(C)													
1.	T	2. a,	,b,c,d	3.	a,b,c	4.	b	5.	a	6.	a,b,c	7.	a,b	8.	d
9.	a	10. b)	11.	c	12.	a	13.	a	14.	С	15.	a	16.	b
17.	a	18. b)	19.	c	20.	b	21.	a	22.	b	23.	С	24.	a
25.	b									19)				



ADDITIONAL QUESTION BANK

- Following set notations represent: $-A \subset B$; $x \notin A$; $A \supset B$; $\{0\}$; $A \not\subset B$
 - (A) A is a proper subset of B; x is not an element of A; A contains B; singleton with an only element zero; A is not contained in B
 - (B) A is a proper subset of B; x is an element of A; A contains B; singleton with an only element zero; A is contained in B
 - (C) A is a proper subset of B; x is not an element of A; A does not contains B; contains elements other than zero; A is not contained in B
 - (D) None
- Represent the following sets in set notation: Set of all alphabets in English language set of all odd integers less than 25 set of all odd integers set of positive integers x satisfying the equation $x^2 + 5x + 7 = 0$:
 - (A) $A=\{x:x \text{ is an alphabet in English}\}$, $I=\{x:x \text{ is an odd integer}>25\}$, $I=\{2, 4, 6, 8 \dots\}$ $I = \{x: x^2 + 5x + 7 = 0\}$
 - (B) $A=\{x:x \text{ is an alphabet in English}\}$, $I=\{x:x \text{ is an odd integer}<25\}$, $I=\{1, 3, 5, 7 \dots\}$ $I = \{x: x^2 + 5x + 7 = 0\}$
 - (C) A={x:x is an alphabet in English}, I={x:x is an odd integer £ 25}, I={1, 3, 5, 7} $I = \{x: x^2 + 5x + 7 = 0\}$
 - (D) None
- Re-write the following sets in a set builder form: $A=\{a, e, i, o, u\}$ $B=\{1, 2, 3, 4, ...\}$ C is a set of integers between -15 and 15.
 - (A) A={x:x is a consonant} B={x:x is an irrational number} C={x: $-15 < x < 15 \land x$ is a fraction}
 - (B) A={x:x is a vowel} B={x:x is a natural number} C={x: $-15^3x^315 \land x$ is a whole number}
 - (C) $A=\{x:x \text{ is a vowel}\}\ B=\{x:x \text{ is a natural number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:-15 < x < 15 \land x \text{ is a whole number}\}\ C=\{x:$
 - (D) None
- If $V=\{0, 1, 2, ...9\}$, $X=\{0, 2, 4, 6, 8\}$, $Y=\{3, 5, 7\}$ and $Z=\{3, 7\}$ then $Y \cup Z$, $(V \cup Y) \cap X$, $(X \cup Z) \cup V$ are respectively: –
 - (A) {3, 5, 7}, {0, 2, 4, 6, 8}, {0, 1, 2, ...9} (B) {2, 4, 6}, {0, 2, 4, 6, 8}, {0, 1, 2, ...9}
 - (C) {2, 4, 6}, {0, 1, 2, ...9}, {0, 2, 4, 6, 8} (D) None
- In question No.(4) $(X \cup Y) \cap Z$ and $(\phi UV)I\phi$ are respectively:
 - (A) $\{0, 2, 4, 6, 8\}, \phi$ (B) $\{3, 7\}, \phi$
- (C) $\{3, 5, 7\}, \phi$
- (D) None



ο.	If $V = \{X: \} K = \{X: \} $	and $S=\{x: \}$ then V ,	K, S are equal	for the value	or x equal to	•
	(A) 0	(B) −1	(C) -2	2	(D) None	
7.		-	0		letter in the word flow wolf} D={x:x is a letter	
	(A) B=C=D and a	all these are subsets	of the set A			
	(B) B=C≠D	(C) $B\neq C\neq D$	(D) N	one		
8.		correctness or other, d \subset {a, c, d} (iii) {I		_	ments: – (i) $\{a, b, c\} = \{0, d\}$	e, b,
	(A) Only (iv) is in	correct	(B) (i) (ii)	are incorrect		
	(C) (ii) (iii) are inc	correct	(D) All a	re incorrect		
9.	statements are con		$D \neq C$ (iii) $C =$	⊃ E (iv) D E (v	which of the follows $D \subset B$ (vi) $D = A$ (vi) $A \subset A$	_
	(A) (i) (ii) (iii) (ix)	(x) (xiii) only are co	orrect (B) (i	ii) (iii) (iv) (x) ((xii) (xiii) only are cor	rect
	(C) (i) (ii) (iv) (ix)	(xi) (xiii) only are c	orrect (D) I	None		
10.	A and $x \in B$ } state		wing statemer	nts are true: -	300 years old}, $F = \{x \mid (i) A \subset B (ii) B = F (ii) \}$	
	(A) (i) (iii) (iv) and	d (v) only are true	(B) (i) (ii)	(iii) and (iv) a	are true	
	(C) (i) (ii) (iii) and	(vi) only are true	(D) None			
11.		which of the following $1 \subset A \text{ (vi) } \{0\} \in A$	~	s are true: – (i)	$\{1\} \subset A \text{ (ii) } \{1\} \in A \text{ (ii) } \{1\}$	ii) ¢
	(A) (i) (iv) and (vi	i) only are true	(B) (i) (iv)) and (vi) only	are true	
	(C) (ii) (iii) and (v	i) only are true	(D) None)		
12.	$= \{y: y = a^2; \text{ a is an}\}$	O .	{x:x is a positi		$X = \{1, 2, 3, \dots 500\}$ (i ltiple of 2} (iv) $B = \{x: x \in A\}$	
	(A) finite infinite	infinite empty	(B) infinit	te infinite finit	e empty	
	(C) infinite finite	infinite empty	(D) None	<u>)</u>		
13.	If $A = \{1, 2, 3, 4\}$	$B = \{2, 3, 7, 9\}$ and ($C = \{1, 4, 7, 9\}$	then		
	(A) $A \cap B \neq \emptyset B$	$\cap C \neq \phi A \cap C \neq \phi b$	out $A \cap B \cap C$	$C = \phi$		
	(B) $A \cap B = \phi B$	$\cap C = \phi A \cap C = \phi$	$A \cap B \cap C = 0$	\$		
	(C) $A \cap B \neq \phi B$	$\cap C \neq \phi A \cap C \neq \phi$	$A \cap B \cap C \neq 0$	\$		
	(D) None					

 $\{2, 5, 6\}$ are subsets of X the set $A \cup (B \cap C)$ is _____.

	(A) {3, 4, 6, 12}	(B) {1, 6, 9, 10}	(C) {2, 5, 6, 11}	(D) None
15.	As per question No.(14) the set $(A \cup B) \cap (A \cup B)$	$(A \cup C)$ is	
	(A) {3, 4, 6, 12}	(B) {1, 6, 9, 10}	(C) {2, 5, 6, 11}	(D) None
16.	groups < Rs.6000/-, R above No. TV set is ava	s.6000/- to Rs.10999 ailable to 70, 50, 20, 5	es was surveyed and not 9/-, Rs.11000/-, to Rs.15 50 families one set is avai ble to 10, 174, 84, 94 fam	5999/-, Rs.16000 and lable to 152, 308, 114,
	$C = \{x \mid x \text{ is a family } w\}$	ith income less than $-$ }, $E = \{x \mid x \text{ is a fam} \}$	ore sets}, $B = \{x \mid x \text{ is a } Rs.6000/-\}$, $D = \{x \mid x \mid \text{ is a } rily \text{ with income Rs. } 110000000000000000000000000000000000$	a family with income
	(ii) $A \cup E$			
	(A) 152, 580	(B) 152, 20	(C) 152, 50	(D) 152, 496
17.	As per question No.(16) find the number of	families in each of the fo	ollowing sets: -
	(i) $(A \cup B)' \cap E$ (ii) $(C \cup B)' \cap E$	$\cup D \cup E) \cap (A \cup B)'$	V. 3	
	(A) 20, 50	(B) 152, 20	(C) 152, 50	(D) 20, 140
18.	As per question No.(16) express the followi	ng sets in set notation: -	
	(i) $\{x \mid x \text{ is a family with } $	n one set and income	e of less than Rs.11000/-}	
	(ii) $\{x \mid x \text{ is a family with}\}$	h no set and income	over Rs.16000/-}	
	$(A)\ (C\cup D)\cap B$	(B	$) (A \cup B)' \cap (C' \cup D' \cup B')$	Ε΄)
	(C) Both	(D) None	
19.	As per question No.(16) express the followi	ng sets in set notation: -	
	(i) $\{x \mid x \text{ is a family with } $	n two or more sets o	r income of Rs.11000/- to	o Rs.15999/-}
	(ii) $\{x \mid x \text{ is a family with}\}$	h no set}		
	$(A) (A \cup E)$	(B) $(A \cup B)'$	(C) Both	(D) None
20.	If $A = \{a, b, c, d\}$ list the	e element of power s	eet P (A)	
	(A) $\{\phi \{a\} \{b\}(\{c\} \{d\} \{a,$	b} {a, c} {a, d} {b, c}	[b, d] {c, d}	
	(B) {a, b, c} {a, b, d} {a,	c, d} {b, c, d}		
	(C) $\{a, b, c, d\}$			
	(D) All the above element	ents are in P (A)		
21.		prevails list the wir	ing body are in a meeting ing coalitions. Given tha	O 1

14. If the universal set is $X = \{x: x \in N | 1 \le x \le 12\}$ and $A = \{1, 9, 10\}$ $B = \{3, 4, 6, 11, 12\}$ and $C = \{1, 9, 10\}$ $A = \{1, 9, 10\}$



(A) {a, b} {a, c} {a, d} {a, b, c} {a, b, d} {a, b, c, d} (B) $\{b, c, d\}$ (C) $\{b, c\}$ $\{b, d\}$ $\{c, d\}$ $\{a, c, d\}$ $\{b, c, d\}$ $\{a\}$ $\{b\}$ $\{c\}$ $\{d\}$ \emptyset (D) None 22. As per question No.(21) with same order of options (A) (B) (C) and (D) list the blocking conditions. 23. As per question No.(21) with same order of options (A) (B) (C) and (D) list the losing conditions. 24. If A ={a, b, c, d, e, f} B = {a, e, i, o, u} and C = {m, n, o, p, q, r, s, t, u} then A \cup B is (A) {a, b, c, d, e, f, i, o, u} (B) $\{a, b, c, i, o, u\}$ (C) $\{d, e, f, i, o, u\}$ (D) None 25. As per question No.(24) A \cup C is (A) {a, b, c, d, e, f, m, n, o, p, q, r, s, t, u} (B) {a, b, c, s, t, u} (C) $\{d, e, f, p, q, r\}$ (D) None 26. As per question No.(24) B \cup C is (A) {a, e, i, o, u, m, n, p, q, r, s, t} (B) $\{a, e, i, r, s, t\}$ (D) None (C) $\{i, o, u, p, q, r\}$ 27. As per question No.(24) A + B is (A) {b, c, d, f} (B) $\{a, e, i, o\}$ (C) $\{m, n, p, q\}$ (D) None 28. As per question No.(24) A \cap B is (A) {a, e} $(C) \{0, u\}$ (B) {i, o} (D) None 29. As per question No.(24) B \cap C is $(A) \{a, e\}$ $(C) \{o, u\}$ (D) None (B) $\{i, o\}$ 30. As per question No.(24) A \cup (B - C) is (B) {a, b, c, d, e, f, o} (C) {a, b, c, d, e, f, u} (A) {a, b, c, d, e, f, i} (D) None 31. As per question No.(24) A \cup B \cup C is (A) {a, b, c, d, e, f, i, o, u, m, n, p, q, r, s, t} (B) {a, b, c, r, s, t} (C) $\{d, e, f, n, p, q\}$ (D) None 32. As per question No.(24) $A \cap B \cap C$ is (A) (B) {a, e} $(C) \{ m, n \}$ (D) None 33. If $A = \{3, 4, 5, 6\}$ $B = \{3, 7, 9, 5\}$ and $C = \{6, 8, 10, 12, 7\}$ then A' is (given that the universal set $U = \{3, 4,, 11, 12, 13\}$ (A) {7, 8,12, 13} (B) {4, 6, 8, 10,13}

(D) None

(C) { 3, 4, 5, 9, 11, 13}

- 34. As per question No.(33) with the same order of options (A) (B) (C) and (D) the set B' is
- 35. As per question No.(33) with the same order of options (A) (B) (C) and (D) the set C' is
- 36. As per question No.(33) the set (A')' is
 - (A) {3, 4, 5, 6}
- (B) {3, 7, 9, 5}
- (C) {8, 10, 11, 12, 13}
- (D) None

- 37. As per question No.(33) the set (B')' is
 - (A) {3, 4, 5, 6}
- (B) {3, 7, 9, 5}
- (C) {8, 10, 11, 12, 13}
- (D) None

- 38. As per question No.(33) the set $(A \cup B)'$ is
 - (A) {3, 4, 5, 6}
- (B) {3, 7, 9, 5}
- (C) {8, 10, 11, 12, 13}
- (D) None

- 39. As per question No.(33) the set $(A \cap B)'$ is
 - (A) {8, 10, 11, 12, 13} (B) {4, 6, 7,13}
- (C) {3, 4, 5, 7, 8,....13}
- (D) None

- 40. As per question No.(33) the set $A' \cup C'$ is
 - (A) {8, 10, 11, 12, 13} (B) {4, 6, 7,13} (C) {3, 4, 5, 7, 8,....13} (D) None

- 41. If $A = \{1, 2, ...9\}$, $B = \{2, 4, 6, 8\}$ $C = \{1, 3, 5, 7, 9\}$, $D = \{3, 4, 5\}$ and $E = \{3, 5\}$ what is set S if it is also given that $S \subset D$ and $S \not\subset B$
 - (A) {3, 5}
- (B) {2, 4}
- (C) {7, 9}
- (D) None
- 42 As per question No.(41) what is set S if it is also given that $S \subset B$ and $S \not\subset C$
 - (A) {3, 5}
- (B) {2, 4}
- (C) {7, 9}
- (D) None
- 43. If $U = \{1, 2, ...9\}$ be the universal set $A = \{1, 2, 3, 4\}$ and $B = \{2, 4, 6, 8\}$ then the set $A \cup B$ is
 - (A) {1, 2, 3, 4, 6, 8}
- (B) {2, 4}
- (C) {5, 6, 7, 8, 9}
- (D) {5, 7, 9}
- 44. As per question No.(43) with the same order of options (A) (B) (C) and (D) the set $A \cap B$ is
- 45. As per question No.(43) with the same order of options (A) (B) (C) and (D) the set A' is
- 46. As per question No.(43) with the same order of options (A) (B) (C) and (D) the set $(A \cup B)'$ is
- 47. As per question No.(43) the set $(A \cap B)'$ is
 - (A) {1, 2, 3, 4, 6, 8}
- (B) {2, 4}
- (C) {5, 6, 7, 8, 9}
- (D) {1, 3, 5, 6, 7, 9}
- 48. Let P = (1, 2, x), Q = (a x y), R = (x, y, z) then $P \times Q$ is
 - (A) $\{(1, a) (1, x) (1, y); (2, a) (2, x) (2, y); (x, a) (x, x) (x, y)\}$
 - (B) $\{(1, x); (1, y); (1, z); (2, x); (2, y); (2, z); (x, x) (x, y) (x, z)\}$
 - (C) $\{(a, x) (a, y) (a, z); (x, x) (x, y) (x, z); (y, x) (y, y) (y, z)\}$
 - (D) $\{(1, x) (1, y) (2, x) (2, y) (x, x) (x, y)\}$
- 49. As per question No.(48) with the same order of options (A) (B) (C) and (D) then the set $P \times R$ is
- 50. As per question No.(48) with the same order of options (A) (B) (C) and (D) then the set $Q \times R$ is



51.	As per question No.(48) with the same order of options (A) (B) (C) and (D) then the set $(P \times Q) \cap (P \times R)$ is										
52.	As per question No.(48) the set $(R \times Q) \cap (R \times P)$ is										
	(A) $\{(a, x) (a, y) (a, z);$	(x, x) (x, y) (x, z); (y, z)	(x) (y, y) (y, z)								
	(B) {(1, x) (1, y) (2, x)	(2, y) (x, x) (x, y)									
	(C) $\{(x, x) (y, x) (z, x)\}$	}									
	(D) {(1, a) (1, x) (1, y) (z, 2) (z, x)}	(2, a) (2, x) (2, y) (x, a	a) (x, x) (x, y) (x, 1) (x, 2)	(y, 1) (y, 2) (y, x) (z, 1)							
53.	As per question No.(4 No.(52) the set $(P \times Q)$		er of options (A) (B) (C)	and (D) as in question							
54.	If P has three elements set $P \times Q \times R$ will have		ow many elements does	the Cartesian product							
	(A) 24	(B) 9	(C) 29	(D) None							
55.	Identify the elements (6, 1) (6, 2) (6, 3)}	of P if set $Q = \{1, 2, 3\}$	and $P \times Q = \{(4, 1) (4, 2)\}$	(4, 3) (5, 1)(5, 2) (5, 3)							
	(A) {3, 4, 5}	(B) {4, 5, 6}	(C) {5, 6, 7}	(D) None							
56.	If $A = \{2, 3\}, B = \{4, 5\}$, C = $\{5, 6\}$ then A \times	(B U C) is								
	(A) {(2, 4) (2, 5) (2, 6) (3, 4) (3, 5) (3, 6)}										
	(B) $\{(2, 5) (3, 5)\}$										
	(C) {(2, 4) (2, 5) (3, 4)	(3, 5) (4, 5) (4, 6) (5,	5) (5, 6)}								
	(D) None										
57.	As per question No. $(A \times (B \cap C))$ is	(56) with the same (order of options (A) (B) (C) and (D) the set							
58.	As per question No.(56 $(B \times C)$ is	6) with the same order	r of options (A) (B) (C) an	d (D) the set (A \times B) \cup							
59.	If A has 32 elements B elements in $A \cap B$	B has 42 elements ar	nd A∪B has 62 elemen	ts find the number of							
	(A) 74	(B) 62	(C) 12	(D) None							
60.		•	8000 read Telegraph and y do not read any paper								
	(A) 3000	(B) 2000	(C) 4000	(D) None							
61.	_	ocoa and 30% coffee a	a and 64% cocoa. Of the and cocoa. Only 6% did r								
	(A) 360	(B) 280	(C) 160	(D) None							

- 62. As per question No.(61) with the same order of options (A) (B) (C) and (D) find the number having tea and cocoa but not coffee.
- 63. As per question No.(61) with the same order of options (A) (B) (C) and (D) find the number having only coffee.
- 64. Complaints about works canteen had been about Mess (M) Food (F) and Service (S). Total complaints 173 were received as follows: –

n(M) = 110, n(F) = 55, n(S) = 67, $n(M \cap F \cap S') = 20$, $n(M \cap S \cap F') = 11$ and $n(F \cap S \cap M') = 16$. Determine the complaints about all the three.

(A) 6

- (B) 53
- (C) 35

- (D) None
- 65. As per question No.(64) with the same order of options (A) (B) (C) and (D) determine the complaints about two or more than two.
- 66. Out of total 150 students 45 passed in Accounts 50 in Maths. 30 in Costing 30 in both Accounts and Maths. 32 in both Maths and Costing 35 in both Accounts and Costing. 25 students passed in all the three subjects. Find the number who passed at least in any one of the subjects.
 - (A) 63

- (B) 53
- (C) 73

- (D) None
- 67. After qualifying out of 400 professionals, 112 joined industry, 120 started practice and 160 joined as paid assistants. There were 32, who were in both practice and service 40 in both practice and assistantship and 20 in both industry and assistantship. There were 12 who did all the three. Find how many could not get any of these.
 - (A) 88

- (B) 244
- (C) 122

- (D) None
- 68. As per question No.(67) with the same order of options (A) (B) (C) and (D) find how many of them did only one of these.
- 69. A marketing research team interviews 100 people about their drinking habits of tea coffee or milk or A B C respectively. Following data is obtained but the Manager is not sure whether these are consistent.

Category	No.	Category	No.
ABC	3	A	42
AB	7	В	17
BC	13	C	27
AC	18		

- (A) Inconsistent since $42 + 17 + 27 7 13 18 + 3 \neq 50$
- (B) Consistent
- (C) Cannot determine due to data insufficiency
- (D) None



70.	On a survey of 100 boys it was found that 50 used white shirt 40 red and 30 blue. 20 were
	habituated in using both white and red shirts 15 both red and blue shirts and 10 blue and
	white shirts. Find the number of boys using all the colours.

(A) 20

- (B) 25
- (C) 30

- (D) None
- 71 As per question No.(70) if 10 boys did not use any of the white red or blue colours and 20 boys used all the colours offer your comments.
 - (A) Inconsistent since $50 + 40 + 30 20 15 10 + 20 \neq 100$
 - (B) Consistent
 - (C) cannot determine due to data insufficiency
 - (D) None
- 72. Out of 60 students 25 failed in paper (1) 24 in paper (2) 32 in paper (3) 9 in paper (1) alone 6 in paper (2) alone 5 in papers (2) and (3) and 3 in papers (1) and (2). Find how many failed in all the three papers.
 - (A) 10

- **(B)** 60
- (C) 50

- (D) None
- 73. As per question No.(72) how many passed in all the three papers?
 - (A) 10

- (B) 60
- (C) 50

- (D) None
- 74. Asked if you will cast your vote for a party the following feed back is obtained: -

	Yes	Don't know
Adult Male	10	5
Adult Female	20 15	5
Youth over 18 years	10 5	10

If A = set of Adult Males C = Common set of Women and Youth Y = set of positive opinion N = set of negative opinion then n(A') is

(A) 25

- (B) 40
- (C) 20

- (D) None
- 75. As per question No.(74) with the same order of options (A) (B) (C) and (D) the set $n(A \cap C)$ is
- 76. As per question No.(74) with the same order of options (A) (B) (C) and (D) the set $n(Y \cup N)'$ is
- 77. As per question No.(74) with the same order of options (A) (B) (C) and (D) the set $n[A \cap (Y \cap N)']$ is
- 78. In a market survey you have obtained the following data which you like to examine regarding its correctness:

Did not use the brand	April	May	June	April & May	May & June	April & June	April May June
Percentage answering 'Yes'	59	62	62	35	33	31	22

- (A) Inconsistent since $59 + 62 + 62 35 33 31 + 22 \neq 100$
- (B) Consistent
- (C) cannot determine due to data insufficiency
- (D) None
- 79. In his report an Inspector of an assembly line showed in respect of 100 units the following which you are require to examine.

Defect	Strength (S)	Flexibility (F)	Radius (R)	S and F	S and R	F and R	SFR
No. of pieces	35	40	18	7	11	12	3

- (A) No. of pieces with radius defect alone was -2 which was impossible
- (B) Report may be accepted
- (C) Cannot be determined due to data insufficiency (D) None
- 80. A survey of 1000 customers revealed the following in respect of their buying habits of different grades:

A grade only	A and C grades	9888	A grade but not B grade	A grade	C and B grades	None
180	80	480	230	360	80	140

How many buy B grade?

- (A) 280
- (B) 400
- (C) 50

- (D) None
- 81. As per question No.(80) with the same order of options (A) (B) (C) and (D) how many buy C grade if and only if they do not buy B grade?
- 82. As per question No.(80) with the same order of options (A) (B) (C) and (D) how many buy C and B grades but not the A grade?
- 83. Consider the following data: -

	Skilled & Direct Worker	Unskilled & Direct Worker	Skilled & Indirect Worker	Unskilled & Indirect Worker
Short Term	6	8	10	20
Medium Term	7	10	16	9
Long Term	3	2	8	0

If S M L T I denote short medium long terms skilled and indirect workers respectively find the number of workers in set M.

(A) 42

- (B) 8
- (C) 10

- (D) 43
- 84. Consider the problem No.(83) and find the number of workers in set $L \cap I$.
 - (A) 42

- (B) 8
- (C) 10

(D) 43



85.	Consider the problem No.(83) and find the number of workers in set $S \cap T \cap I$.								
	(A) 42	(B) 8	(C) 10	(D) 43					
86.	Consider the problem	No.(83) and find the	number of workers in se	t					
86. (87. (88. (89. (90. (91. 4	$(M \cup L) \cap (T \cup I).$								
	(A) 42	(B) 8	(C) 10	(D) 43					
87.	Consider the problem	No.(83) and find the	number of workers in se	t					
	$S' \cup (S' \cap I)'.$								
	(A) 42	(B) 44	(C) 43	(D) 99					
88.	Consider the problem members. Pair is $(S \cup I)$		hich set of the pair has	more workers as its					
	(A) $(S \cup M)' > L$	(B) $(S \cup M)' < L$	(C) $(S \cup M)' = L$	(D) None					
89.	Consider the problem members. Pair is (I \cap T		hich set of the pair has	more workers as its					
(A) 86. Co (M) (A) 87. Co (A) 88. Co (A) 89. Co (A) (C) 90. Out in Fir (A) 91. As (A) 92. As (A) 93. As (A) 94. As (A) 95. As	(A) $(I \cap T)' > [S - (I \cap T)]$	(B)	$(I \cap T)' < [S - (I \cap S')]$						
	(C) $(I \cap T)' = [S - (I \cap T)]$	S')] (D) None						
90.		oup-II, 372 in group-l	gate, 166 in the aggregate, 590 in group-II and 12	0 1					
() (87. C) (88. C) (89. C) (90. C) (191. A) (92. A) (93. A) (94. A) (95. A)	(A) 106	(B) 224	(C) 206	(D) 464					
91.	As per question No.(90	0) how many failed ir	n the aggregate but not in	n group-II?					
	(A) 106	(B) 224	(C) 206	(D) 464					
	As per question No.(90) how many failed in group-I but not in the aggregate?								
	(A) 106	(B) 224	(C) 206	(D) 464					
93.	As per question No.(90) how many failed in group-II but not in group-I?								
	(A) 106	(B) 224	(C) 206	(D) 464					
94.	As per question No.(90	0) how many failed ir	aggregate or group-II b	ut not in group-I?					
	(A) 206	(B) 464	(C) 628	(D) 164					
95.	As per question No.(90) how many failed in aggregate but not in group-I and group-II?								
	(A) 206	(B) 464	(C) 628	(D) 164					



ANSWERS

1)	A	2)	В	3)	C	4)	A	5)	В	6)	С
7)	A	8)	A	9)	A	10)	В	11)	A	12)	A
13)	A	14)	В	15)	В	16)	D	17)	D	18)	С
19)	C	20)	D	21)	A	22)	В	23)	C	24)	A
25)	A	26)	A	27)	A	28)	A	29)	C	30)	A
31)	A	32)	A	33)	A	34)	В	35)	C	36)	A
37)	В	38)	C	39)	В	40)	C	41)	A	42)	В
43)	A	44)	В	45)	C	46)	D	47)	D	48)	A
49)	В	50)	C	51)	D	52)	C	53)	D	54)	A
55)	В	56)	A	57)	В	58)	С	59)	C	60)	A
61)	A	62)	В	63)	Cilling	64)	A	65)	В	66)	В
67)	A	68)	В	69)	A	70)	B	71)	A	72)	A
73)	A	74)	A	75)	В	76)	C	77)	C	78)	A
79)	A	80)	A	81)	В	82)	C	83)	A	84)	В
85)	C	86)	D	87)	D	88)	(C>)	89)	A	90)	A
91)	В	92)	C	93)	D	94)	5	95)	D		
				_	With.		- William				